1. Determine the perimeter and area of rectangles A and B.

   a. \( A = \) ____________
   
   b. \( P = \) ____________

2. Determine the perimeter and area of each rectangle.

   a. \( A = \) ____________
   
   b. \( P = \) ____________
3. Determine the perimeter of each rectangle.
   a. ![Rectangle A]
      \[ P = \text{__________} \]
   b. ![Rectangle B]
      \[ P = \text{__________} \]

4. Given the rectangle’s area, find the unknown side length.
   a. ![Rectangle C]
      \[ x = \text{__________} \]
   b. ![Rectangle D]
      \[ x = \text{__________} \]
5. Given the rectangle’s perimeter, find the unknown side length.
   a. \( P = 120 \text{ cm} \)  
   b. \( P = 1,000 \text{ m} \)

   \[
x = \underline{\phantom{0000}}
   \]

6. Each of the following rectangles has whole number side lengths. Given the area and perimeter, find the length and width.
   a. \( P = 20 \text{ cm} \)
   b. \( P = 28 \text{ m} \)

   \[
   l = \underline{\phantom{0000}} \\
   w = \underline{\phantom{0000}}
   \]

Lesson 1: Investigate and use the formulas for area and perimeter of rectangles.
1. Determine the perimeter and area of rectangles A and B.

   \[ A = \quad \text{cm}^2 \]
   \[ P = \quad \text{cm} \]

   a. \[ A = \quad \text{cm}^2 \]
   \[ P = \quad \text{cm} \]

   b. \[ A = \quad \text{cm}^2 \]
   \[ P = \quad \text{cm} \]

2. Determine the perimeter and area of each rectangle.

   a. \[ A = \quad \text{cm}^2 \]
   \[ P = \quad \text{cm} \]

   b. \[ A = \quad \text{cm}^2 \]
   \[ P = \quad \text{cm} \]
3. Determine the perimeter of each rectangle.
   a. \[ P = \, \quad \text{cm} \]
   b. \[ P = \, \quad \text{cm} \]

4. Given the rectangle’s area, find the unknown side length.
   a. \[ x \, = \, \quad \text{cm} \]
   b. \[ x \, = \, \quad \text{m} \]

Lesson 1: Investigate and use the formulas for area and perimeter of rectangles.
5. Given the rectangle’s perimeter, find the unknown side length.
   a. P = 180 cm
   b. P = 1,000 m

   ![Rectangle with unknown side length](image)

   \[ x = \text{___________} \]  \[ x = \text{___________} \]

6. Each of the following rectangles has whole number side lengths. Given the area and perimeter, find the length and width.
   a. A = 32 square cm  P = 24 cm
   b. A = 36 square m  P = 30 m

   ![Rectangle with unknown side length](image)

   \[ l = \text{___________} \]  \[ w = \text{___________} \]
   \[ l = \text{___________} \]  \[ w = \text{___________} \]
Lesson 2: Solve multiplicative comparison word problems by applying the area and perimeter formulas.

Name ____________________________ Date ____________________

1. A rectangular porch is 4 feet wide. It is 3 times as long as it is wide.
   a. Label the diagram with the dimensions of the porch.

   [Diagram]

   b. Find the perimeter of the porch.

2. A narrow rectangular banner is 5 inches wide. It is 6 times as long as it is wide.
   a. Draw a diagram of the banner, and label its dimensions.

   [Diagram]

   b. Find the perimeter and area of the banner.
3. The area of a rectangle is 42 square centimeters. Its length is 7 centimeters.
   a. What is the width of the rectangle?
   
   b. Charlie wants to draw a second rectangle that is the same length but is 3 times as wide. Draw and label Charlie’s second rectangle.
   
   c. What is the perimeter of Charlie’s second rectangle?
4. The area of Betsy’s rectangular sandbox is 20 square feet. The longer side measures 5 feet. The sandbox at the park is twice as long and twice as wide as Betsy’s.

   a. Draw and label a diagram of Betsy’s sandbox. What is its perimeter?
   
   b. Draw and label a diagram of the sandbox at the park. What is its perimeter?

   c. What is the relationship between the two perimeters?

   d. Find the area of the park’s sandbox using the formula $A = l \times w$. 
Lesson 2 Problem Set

e. The sandbox at the park has an area that is how many times that of Betsy’s sandbox?

f. Compare how the perimeter changed with how the area changed between the two sandboxes. Explain what you notice using words, pictures, or numbers.
1. A rectangular pool is 7 feet wide. It is 3 times as long as it is wide.
   a. Label the diagram with the dimensions of the pool.
      
      
   b. Find the perimeter of the pool.

2. A poster is 3 inches long. It is 4 times as wide as it is long.
   a. Draw a diagram of the poster, and label its dimensions.

   b. Find the perimeter and area of the poster.
3. The area of a rectangle is 36 square centimeters, and its length is 9 centimeters.

   a. What is the width of the rectangle?

   b. Elsa wants to draw a second rectangle that is the same length but is 3 times as wide. Draw and label Elsa’s second rectangle.

   c. What is the perimeter of Elsa’s second rectangle?
4. The area of Nathan’s bedroom rug is 15 square feet. The longer side measures 5 feet. His living room rug is twice as long and twice as wide as the bedroom rug.

   a. Draw and label a diagram of Nathan’s bedroom rug. What is its perimeter?
   b. Draw and label a diagram of Nathan’s living room rug. What is its perimeter?

   c. What is the relationship between the two perimeters?

   d. Find the area of the living room rug using the formula $A = l \times w$. 

Lesson 2: Solve multiplicative comparison word problems by applying the area and perimeter formulas.
e. The living room rug has an area that is how many times that of the bedroom rug?

f. Compare how the perimeter changed with how the area changed between the two rugs. Explain what you notice using words, pictures, or numbers.
Solve the following problems. Use pictures, numbers, or words to show your work.

1. The rectangular projection screen in the school auditorium is 5 times as long and 5 times as wide as the rectangular screen in the library. The screen in the library is 4 feet long with a perimeter of 14 feet. What is the perimeter of the screen in the auditorium?

2. The width of David’s rectangular tent is 5 feet. The length is twice the width. David’s rectangular air mattress measures 3 feet by 6 feet. If David puts the air mattress in the tent, how many square feet of floor space will be available for the rest of his things?
3. Jackson’s rectangular bedroom has an area of 90 square feet. The area of his bedroom is 9 times that of his rectangular closet. If the closet is 2 feet wide, what is its length?

4. The length of a rectangular deck is 4 times its width. If the deck’s perimeter is 30 feet, what is the deck’s area?
Solve the following problems. Use pictures, numbers, or words to show your work.

1. Katie cut out a rectangular piece of wrapping paper that was 2 times as long and 3 times as wide as the box that she was wrapping. The box was 5 inches long and 4 inches wide. What is the perimeter of the wrapping paper that Katie cut?

2. Alexis has a rectangular piece of red paper that is 4 centimeters wide. Its length is twice its width. She glues a rectangular piece of blue paper on top of the red piece measuring 3 centimeters by 7 centimeters. How many square centimeters of red paper will be visible on top?
3. Brinn’s rectangular kitchen has an area of 81 square feet. The kitchen is 9 times as many square feet as Brinn’s pantry. If the rectangular pantry is 3 feet wide, what is the length of the pantry?

4. The length of Marshall’s rectangular poster is 2 times its width. If the perimeter is 24 inches, what is the area of the poster?
Lesson 4: Interpret and represent patterns when multiplying by 10, 100, and 1,000 in arrays and numerically.
Draw place value disks and arrows to represent each product.

4. \(12 \times 10 = \underline{\phantom{0000}}\)

\((1 \text{ ten } 2 \text{ ones}) \times 10 = \underline{\phantom{0000}}\)

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5. \(18 \times 100 = \underline{\phantom{0000}}\)

\(18 \times 10 \times 10 = \underline{\phantom{0000}}\)

\((1 \text{ ten } 8 \text{ ones}) \times 100 = \underline{\phantom{0000}}\)

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6. \(25 \times 1,000 = \underline{\phantom{0000}}\)

\(25 \times 10 \times 10 \times 10 = \underline{\phantom{0000}}\)

\((2 \text{ tens } 5 \text{ ones}) \times 1,000 = \underline{\phantom{0000}}\)

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Decompose each multiple of 10, 100, or 1,000 before multiplying.

7. \(3 \times 40 = 3 \times 4 \times \underline{\phantom{000}}= 12 \times \underline{\phantom{000}}= \underline{\phantom{0000}}\)

8. \(3 \times 200 = 3 \times \underline{\phantom{000}} \times \underline{\phantom{000}}= \underline{\phantom{0000}} \times \underline{\phantom{0000}}= \underline{\phantom{000000}}\)

9. \(4 \times 4,000 = \underline{\phantom{00000}} \times \underline{\phantom{00000}} \times \underline{\phantom{00000000}}= \underline{\phantom{00000000}} \times \underline{\phantom{00000000}}= \underline{\phantom{00000000}}\)

10. \(5 \times 4,000 = \underline{\phantom{0000000}} \times \underline{\phantom{0000000}} \times \underline{\phantom{000000000}}= \underline{\phantom{000000000}} \times \underline{\phantom{000000000}}= \underline{\phantom{000000000}}\)
Lesson 4: Interpret and represent patterns when multiplying by 10, 100, and 1,000 in arrays and numerically.

Example:

\[ 5 \times 10 = \underline{50} \]
\[ 5 \text{ ones} \times 10 = \underline{5} \text{ tens} \]

Draw place value disks and arrows as shown to represent each product.

1. \( 7 \times 100 = \underline{700} \)

\[ 7 \times 10 \times 10 = \underline{700} \]
\[ 7 \text{ ones} \times 100 = \underline{700} \]

2. \( 7 \times 1,000 = \underline{7,000} \)

\[ 7 \times 10 \times 10 \times 10 = \underline{7,000} \]
\[ 7 \text{ ones} \times 1,000 = \underline{7,000} \]

3. Fill in the blanks in the following equations.

a. \( 8 \times 10 = \underline{80} \)

b. \( \underline{100} \times 8 = 800 \)

c. \( 8,000 = \underline{8} \times 1,000 \)

d. \( 10 \times 3 = \underline{30} \)

e. \( 3 \times \underline{1,000} = 3,000 \)

f. \( \underline{100} \times 3 = 300 \)

g. \( 1,000 \times 4 = \underline{4,000} \)

h. \( \underline{100} = 10 \times 4 \)

i. \( 400 = \underline{4} \times 100 \)
Draw place value disks and arrows to represent each product.

4. $15 \times 10 = \underline{\hspace{2cm}}$

   (1 ten 5 ones) $\times 10 = \underline{\hspace{2cm}}$

5. $17 \times 100 = \underline{\hspace{2cm}}$

   $17 \times 10 \times 10 = \underline{\hspace{2cm}}$

   (1 ten 7 ones) $\times 100 = \underline{\hspace{2cm}}$

6. $36 \times 1,000 = \underline{\hspace{2cm}}$

   $36 \times 10 \times 10 \times 10 = \underline{\hspace{2cm}}$

   (3 tens 6 ones) $\times 1,000 = \underline{\hspace{2cm}}$

Decompose each multiple of 10, 100, or 1,000 before multiplying.

7. $2 \times 80 = 2 \times 8 \times \underline{\hspace{2cm}}$

   $= 16 \times \underline{\hspace{2cm}}$

   $= \underline{\hspace{2cm}}$

8. $2 \times 400 = 2 \times \underline{\hspace{2cm}} \times \underline{\hspace{2cm}}$

   $= \underline{\hspace{2cm}} \times \underline{\hspace{2cm}}$

   $= \underline{\hspace{2cm}}$

9. $5 \times 5,000 = \underline{\hspace{2cm}} \times \underline{\hspace{2cm}} \times \underline{\hspace{2cm}}$

   $= \underline{\hspace{2cm}} \times \underline{\hspace{2cm}}$

   $= \underline{\hspace{2cm}}$

10. $7 \times 6,000 = \underline{\hspace{2cm}} \times \underline{\hspace{2cm}} \times \underline{\hspace{2cm}}$

    $= \underline{\hspace{2cm}} \times \underline{\hspace{2cm}}$

    $= \underline{\hspace{2cm}}$
Lesson 4: Interpret and represent patterns when multiplying by 10, 100, and 1,000 in arrays and numerically.

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thousands place value chart
Name ___________________________________________ Date ________________

Draw place value disks to represent the value of the following expressions.

1. $2 \times 3 = \boxed{6}$
   
   2 times _____ ones is _____ ones.

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   $\times 2$

2. $2 \times 30 = \boxed{60}$
   
   2 times _____ tens is __________.

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   $\times 2$

3. $2 \times 300 = \boxed{600}$
   
   2 times _____ is ______________________.

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   $\times 2$

4. $2 \times 3,000 = \boxed{6,000}$
   
   _____ times ______________________ is ______________________.

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   $\times 2$
5. Find the product.

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<tr>
<td>a. $20 \times 7$</td>
<td>b. $3 \times 60$</td>
<td>c. $3 \times 400$</td>
<td>d. $2 \times 800$</td>
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<tr>
<td>e. $7 \times 30$</td>
<td>f. $60 \times 6$</td>
<td>g. $400 \times 4$</td>
<td>h. $4 \times 8,000$</td>
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<tr>
<td>i. $5 \times 30$</td>
<td>j. $5 \times 60$</td>
<td>k. $5 \times 400$</td>
<td>l. $8,000 \times 5$</td>
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6. Brianna buys 3 packs of balloons for a party. Each pack has 60 balloons. How many balloons does Brianna have?
7. Jordan has twenty times as many baseball cards as his brother. His brother has 9 cards. How many cards does Jordan have?

8. The aquarium has 30 times as many fish in one tank as Jacob has. The aquarium has 90 fish. How many fish does Jacob have?
Draw place value disks to represent the value of the following expressions.

1. $5 \times 2 = \underline{\hspace{1cm}}$
   
   5 times _____ ones is _____ ones.

   
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   2. $5 \times 20 = \underline{\hspace{1cm}}$

   5 times _______ tens is ____________________.

   
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   3. $5 \times 200 = \underline{\hspace{1cm}}$

   5 times ______________ is ____________________.

   
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   4. $5 \times 2,000 = \underline{\hspace{1cm}}$

   ___ times ____________________ is ____________________.

   
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5. Find the product.

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<tbody>
<tr>
<td>a.</td>
<td>20 × 9</td>
<td>b.</td>
<td>6 × 70</td>
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<tr>
<td>c.</td>
<td>7 × 700</td>
<td>d.</td>
<td>3 × 900</td>
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<tr>
<td>e.</td>
<td>9 × 90</td>
<td>f.</td>
<td>40 × 7</td>
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<td>g.</td>
<td>600 × 6</td>
<td>h.</td>
<td>8 × 6,000</td>
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<tr>
<td>i.</td>
<td>5 × 70</td>
<td>j.</td>
<td>5 × 80</td>
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<tr>
<td>k.</td>
<td>5 × 200</td>
<td>l.</td>
<td>6,000 × 5</td>
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6. At the school cafeteria, each student who orders lunch gets 6 chicken nuggets. The cafeteria staff prepares enough for 300 kids. How many chicken nuggets does the cafeteria staff prepare altogether?
7. Jaelynn has 30 times as many stickers as her brother. Her brother has 8 stickers. How many stickers does Jaelynn have?

8. The flower shop has 40 times as many flowers in one cooler as Julia has in her bouquet. The cooler has 120 flowers. How many flowers are in Julia’s bouquet?
Lesson 6 Problem Set

Name ___________________________________________ Date __________________

Represent the following problem by drawing disks in the place value chart.

1. To solve $20 \times 40$, think 

   \[(2 \text{ tens } \times 4) \times 10 = \quad \]

   \[20 \times (4 \times 10) = \quad \]

   \[20 \times 40 = \quad \]

   \[
   \begin{array}{ccc}
   & \text{hundreds} & \text{tens} & \text{ones} \\
   \hline
   \end{array}
   \]

2. Draw an area model to represent $20 \times 40$.

   2 tens \times 4 tens = ____  _________

3. Draw an area model to represent $30 \times 40$.

   3 tens \times 4 tens = ____  _________

   $30 \times 40 = \quad$
4. Draw an area model to represent $20 \times 50$.

$$
2 \text{ tens} \times 5 \text{ tens} = \underline{\quad} \underline{\quad} \\
20 \times 50 = \underline{\quad}
$$

Rewrite each equation in unit form and solve.

5. $20 \times 20 = \underline{\quad}$

$$
2 \text{ tens} \times 2 \text{ tens} = \underline{\quad} \text{ hundreds}
$$

6. $60 \times 20 = \underline{\quad}$

$$
6 \text{ tens} \times 2 \underline{\quad} = \underline{\quad} \text{ hundreds}
$$

7. $70 \times 20 = \underline{\quad}$

$$
\underline{\quad} \text{ tens} \times \underline{\quad} \text{ tens} = 14 \underline{\quad}
$$

8. $70 \times 30 = \underline{\quad}$

$$
\underline{\quad} \underline{\quad} \times \underline{\quad} \underline{\quad} = \underline{\quad} \text{ hundreds}
$$
9. If there are 40 seats per row, how many seats are in 90 rows?

10. One ticket to the symphony costs $50. How much money is collected if 80 tickets are sold?
Name ___________________________________________________________________________ Date _________________

Represent the following problem by drawing disks in the place value chart.

1. To solve \(30 \times 60\), think

\[
(3 \text{ tens} \times 6) \times 10 = \underline{______}
\]
\[
30 \times (6 \times 10) = \underline{______}
\]
\[
30 \times 60 = \underline{______}
\]

2. Draw an area model to represent \(30 \times 60\).

\[
3 \text{ tens} \times 6 \text{ tens} = \underline{______} \quad \underline{______}
\]

3. Draw an area model to represent \(20 \times 20\).

\[
2 \text{ tens} \times 2 \text{ tens} = \underline{______} \quad \underline{______}
\]
\[
20 \times 20 = \underline{______}
\]
4. Draw an area model to represent $40 \times 60$.

$$4 \text{ tens} \times 6 \text{ tens} = \underline{} \quad \underline{}$$

$$40 \times 60 = \underline{}$$

Rewrite each equation in unit form and solve.

5. $50 \times 20 = \underline{}$

5 tens $\times$ 2 tens = _____ hundreds

6. $30 \times 50 = \underline{}$

3 tens $\times$ 5 _______ = ____ hundreds

7. $60 \times 20 = \underline{}$

_____ tens $\times$ _____ tens = 12 ________

8. $40 \times 70 = \underline{}$

_____ _____ $\times$ _____ _____ = _____ hundreds
9. There are 60 seconds in a minute and 60 minutes in an hour. How many seconds are in one hour?

10. To print a comic book, 50 pieces of paper are needed. How many pieces of paper are needed to print 40 comic books?
Lesson 7 Problem Set

Name ____________________________ Date __________________

1. Represent the following expressions with disks, regrouping as necessary, writing a matching expression, and recording the partial products vertically as shown below.

   a. $1 \times 43$

      | tens | ones |
      |------|------|
      | 4    | 3    |

      \[ \begin{array}{c}
      \times 1 \\
      \hline
      3 \quad \rightarrow 1 \times 3 \text{ ones} \\
      + 4 0 \quad \rightarrow 1 \times 4 \text{ tens} \\
      \hline
      4 3
      \end{array} \]

   b. $2 \times 43$

      | tens | ones |
      |------|------|
      |      |      |

   c. $3 \times 43$

      | hundreds | tens | ones |
      |----------|------|------|
      |          |      |      |
d. 4 × 43

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2. Represent the following expressions with disks, regrouping as necessary. To the right, record the partial products vertically.

a. 2 × 36

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b. 3 × 61

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c. 4 × 84

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Lesson 7 Homework

Name ______________________________ Date __________________

1. Represent the following expressions with disks, regrouping as necessary, writing a matching expression, and recording the partial products vertically.

   a. \(3 \times 24\)
      
      | tens | ones |
      |------|------|
      |      |      |

   b. \(3 \times 42\)
      
      | hundreds | tens | ones |
      |----------|------|------|
      |          |      |      |

   c. \(4 \times 34\)
      
      | hundreds | tens | ones |
      |----------|------|------|
      |          |      |      |
2. Represent the following expressions with disks, regrouping as necessary. To the right, record the partial products vertically.

a. $4 \times 27$

<table>
<thead>
<tr>
<th>hundreds</th>
<th>tens</th>
<th>ones</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

b. $5 \times 42$

<table>
<thead>
<tr>
<th>hundreds</th>
<th>tens</th>
<th>ones</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

3. Cindy says she found a shortcut for doing multiplication problems. When she multiplies $3 \times 24$, she says, “$3 \times 4$ is 12 ones, or 1 ten and 2 ones. Then, there’s just 2 tens left in 24, so add it up, and you get 3 tens and 2 ones.” Do you think Cindy’s shortcut works? Explain your thinking in words, and justify your response using a model or partial products.
Lesson 7: Use place value disks to represent two-digit by one-digit multiplication.

<table>
<thead>
<tr>
<th>ten thousands</th>
<th>thousands</th>
<th>hundreds</th>
<th>tens</th>
<th>ones</th>
</tr>
</thead>
</table>

ten thousands place value chart
1. Represent the following expressions with disks, regrouping as necessary, writing a matching expression, and recording the partial products vertically as shown below.

a. $1 \times 213$

<table>
<thead>
<tr>
<th>hundreds</th>
<th>tens</th>
<th>ones</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

\[
\begin{array}{ccc}
2 & 1 & 3 \\
\times & 1 \\
\end{array} \rightarrow 1 \times 3 \text{ ones}
\]

\[
\begin{array}{ccc}
2 & 1 & 3 \\
\times & 1 \rightarrow 1 \times 1 \text{ ten}
\end{array}
\]

\[
\begin{array}{ccc}
2 & 1 & 3 \\
\times & 1 \rightarrow 1 \times 2 \text{ hundreds}
\end{array}
\]

\[
1 \times \_ \text{ hundreds} + 1 \times \_ \text{ ten} + 1 \times \_ \text{ ones}
\]

b. $2 \times 213$

<table>
<thead>
<tr>
<th>hundreds</th>
<th>tens</th>
<th>ones</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

c. $3 \times 214$

<table>
<thead>
<tr>
<th>hundreds</th>
<th>tens</th>
<th>ones</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
2. Represent the following expressions with disks, using either method shown during class, regrouping as necessary. To the right, record the partial products vertically.

a. \(3 \times 212\)

b. \(2 \times 4,036\)

d. \(3 \times 1,254\)
c. $3 \times 2,546$

d. $3 \times 1,407$

3. Every day at the bagel factory, Cyndi makes 5 different kinds of bagels. If she makes 144 of each kind, what is the total number of bagels that she makes?
1. Represent the following expressions with disks, regrouping as necessary, writing a matching expression, and recording the partial products vertically as shown below.

a. $2 \times 424$

<table>
<thead>
<tr>
<th>hundreds</th>
<th>tens</th>
<th>ones</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

$$\begin{array}{c}
4 \quad 2 \quad 4 \\
\times \quad 2 \\
\hline
\end{array}$$

$\rightarrow 2 \times \Box \text{ ones}$

$\rightarrow 2 \times \Box \text{ }$

$\rightarrow \Box \times \Box \text{ }$

$$2 \times \Box \text{ } + 2 \times \Box \text{ } + 2 \times \Box \text{ ones}$$

b. $3 \times 424$

<table>
<thead>
<tr>
<th>hundreds</th>
<th>tens</th>
<th>ones</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>


c. $4 \times 1,424$

<table>
<thead>
<tr>
<th>hundreds</th>
<th>tens</th>
<th>ones</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
2. Represent the following expressions with disks, using either method shown in class, regrouping as necessary. To the right, record the partial products vertically.

a. $2 \times 617$

b. $5 \times 642$

c. $3 \times 3,034$
3. Every day, Penelope jogs three laps around the playground to keep in shape. The playground is rectangular with a width of 163 m and a length of 320 m.
   a. Find the total amount of meters in one lap.
   b. Determine how many meters Penelope jogs in three laps.
1. Solve using each method.

<table>
<thead>
<tr>
<th>Partial Products</th>
<th>Standard Algorithm</th>
</tr>
</thead>
<tbody>
<tr>
<td>a. 3 4</td>
<td>3 4</td>
</tr>
<tr>
<td>× 4</td>
<td>× 4</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Partial Products</th>
<th>Standard Algorithm</th>
</tr>
</thead>
<tbody>
<tr>
<td>b. 2 2 4</td>
<td>2 2 4</td>
</tr>
<tr>
<td>× 3</td>
<td>× 3</td>
</tr>
</tbody>
</table>

2. Solve. Use the standard algorithm.

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>a. 2 5 1</td>
<td>b. 1 3 5</td>
<td>c. 3 0 4</td>
</tr>
<tr>
<td>× 3</td>
<td>× 6</td>
<td>× 9</td>
</tr>
</tbody>
</table>

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>d. 4 0 5</td>
<td>e. 3 1 6</td>
<td>f. 3 9 2</td>
</tr>
<tr>
<td>× 4</td>
<td>× 5</td>
<td>× 6</td>
</tr>
</tbody>
</table>
3. The product of 7 and 86 is ________.  

4. 9 times as many as 457 is _________.

5. Jashawn wants to make 5 airplane propellers. He needs 18 centimeters of wood for each propeller. How many centimeters of wood will he use?
6. One game system costs $238. How much will 4 game systems cost?

7. A small bag of chips weighs 48 grams. A large bag of chips weighs three times as much as the small bag. How much will 7 large bags of chips weigh?
1. Solve using each method.

<table>
<thead>
<tr>
<th>Partial Products</th>
<th>Standard Algorithm</th>
</tr>
</thead>
<tbody>
<tr>
<td>a. 4 6</td>
<td>4 6</td>
</tr>
<tr>
<td>× 2</td>
<td>× 2</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Partial Products</th>
<th>Standard Algorithm</th>
</tr>
</thead>
<tbody>
<tr>
<td>b. 3 1 5</td>
<td>3 1 5</td>
</tr>
<tr>
<td>× 4</td>
<td>× 4</td>
</tr>
</tbody>
</table>

2. Solve using the standard algorithm.

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>a. 2 3 2</td>
<td>4</td>
<td></td>
</tr>
<tr>
<td>× 4</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>b. 1 4 2</td>
<td>6</td>
<td></td>
</tr>
<tr>
<td>× 4</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>c. 3 1 4</td>
<td>7</td>
<td></td>
</tr>
<tr>
<td>× 7</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>d. 4 4 0</td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>× 3</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>e. 5 0 7</td>
<td>8</td>
<td></td>
</tr>
<tr>
<td>× 8</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>f. 3 8 4</td>
<td>9</td>
<td></td>
</tr>
<tr>
<td>× 9</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
3. What is the product of 8 and 54?

4. Isabel earned 350 points while she was playing Blasting Robot. Isabel’s mom earned 3 times as many points as Isabel. How many points did Isabel’s mom earn?

5. To get enough money to go on a field trip, every student in a club has to raise $53 by selling chocolate bars. There are 9 students in the club. How much money does the club need to raise to go on the field trip?
6. Mr. Meyers wants to order 4 tablets for his classroom. Each tablet costs $329. How much will all four tablets cost?

7. Amaya read 64 pages last week. Amaya’s older brother, Rogelio, read twice as many pages in the same amount of time. Their big sister, Elianna, is in high school and read 4 times as many pages as Rogelio did. How many pages did Elianna read last week?
Lesson 10: Objective: Multiply three- and four-digit numbers by one-digit numbers applying the standard algorithm.

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Name ______________________________</td>
<td>Date ________________</td>
</tr>
</tbody>
</table>

1. Solve using the standard algorithm.

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>a.</strong> $3 \times 42$</td>
<td><strong>b.</strong> $6 \times 42$</td>
</tr>
<tr>
<td><strong>c.</strong> $6 \times 431$</td>
<td><strong>d.</strong> $3 \times 431$</td>
</tr>
<tr>
<td><strong>e.</strong> $3 \times 6,212$</td>
<td><strong>f.</strong> $3 \times 3,106$</td>
</tr>
<tr>
<td><strong>g.</strong> $4 \times 4,309$</td>
<td><strong>h.</strong> $4 \times 8,618$</td>
</tr>
</tbody>
</table>
2. There are 365 days in a common year. How many days are in 3 common years?

3. The length of one side of a square city block is 462 meters. What is the perimeter of the block?

4. Jake ran 2 miles. Jesse ran 4 times as far. There are 5,280 feet in a mile. How many feet did Jesse run?
Name ________________________________ Date __________________

1. Solve using the standard algorithm.

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>a.</td>
<td>b.</td>
</tr>
<tr>
<td>3 × 41</td>
<td>9 × 41</td>
</tr>
<tr>
<td>c.</td>
<td>d.</td>
</tr>
<tr>
<td>7 × 143</td>
<td>7 × 286</td>
</tr>
<tr>
<td>e.</td>
<td>f.</td>
</tr>
<tr>
<td>4 × 2,048</td>
<td>4 × 4,096</td>
</tr>
<tr>
<td>g.</td>
<td>h.</td>
</tr>
<tr>
<td>8 × 4,096</td>
<td>4 × 8,192</td>
</tr>
</tbody>
</table>
Lesson 10 Homework

2. Robert’s family brings six gallons of water for the players on the football team. If one gallon of water contains 128 fluid ounces, how many fluid ounces are in six gallons?

3. It takes 687 Earth days for the planet Mars to revolve around the sun once. How many Earth days does it take Mars to revolve around the sun four times?

4. Tammy buys a 4-gigabyte memory card for her camera. Dijonea buys a memory card with twice as much storage as Tammy’s. One gigabyte is 1,024 megabytes. How many megabytes of storage does Dijonea have on her memory card?
1. Solve the following expressions using the standard algorithm, the partial products method, and the area model.

   a. \[425 \times 4\]

   \[4 (400 + 20 + 5)\]

   \[(4 \times \underline{\hspace{2cm}}) + (4 \times \underline{\hspace{2cm}}) + (4 \times \underline{\hspace{2cm}})\]

   b. \[534 \times 7\]

   \[7 (\underline{\hspace{2cm}} + \underline{\hspace{2cm}} + \underline{\hspace{2cm}})\]

   \[(\underline{\hspace{2cm}} \times \underline{\hspace{2cm}}) + (\underline{\hspace{2cm}} \times \underline{\hspace{2cm}}) + (\underline{\hspace{2cm}} \times \underline{\hspace{2cm}})\]

   c. \[209 \times 8\]

   \[\underline{\hspace{2cm}} (\underline{\hspace{2cm}} + \underline{\hspace{2cm}})\]

   \[(\underline{\hspace{2cm}} \times \underline{\hspace{2cm}}) + (\underline{\hspace{2cm}} \times \underline{\hspace{2cm}})\]
2. Solve using the partial products method.

Cayla’s school has 258 students. Janet’s school has 3 times as many students as Cayla’s. How many students are in Janet’s school?

3. Model with a tape diagram and solve.

4 times as much as 467

Solve using the standard algorithm, the area model, the distributive property, or the partial products method.

4. \( 5,131 \times 7 \)
5. 3 times as many as 2,805

6. A restaurant sells 1,725 pounds of spaghetti and 925 pounds of linguini every month. After 9 months, how many pounds of pasta does the restaurant sell?
1. Solve the following expressions using the standard algorithm, the partial products method, and the area model.

a. \[302 \times 8\]

\[8 \times (300 + 2)\]

\[8 \times (\_\_ + \_\_)\]

b. \[216 \times 5\]

\[5 \times (\_\_ + \_\_ + \_\_)\]

\[5 \times (\_\_ \times \_\_) + (\_\_ \times \_\_) + (\_\_ \times \_\_)\]

c. \[593 \times 9\]

\[\_\_ \times (\_\_ + \_\_ + \_\_)\]

\[\_\_ \times (\_\_ \times \_\_) + (\_\_ \times \_\_) + (\_\_ \times \_\_)\]
2. Solve using the partial products method.

   On Monday, 475 people visited the museum. On Saturday, there were 4 times as many visitors as there were on Monday. How many people visited the museum on Saturday?

3. Model with a tape diagram and solve.

   6 times as much as 384

Solve using the standard algorithm, the area model, the distributive property, or the partial products method.

4. \(6,253 \times 3\)
5. 7 times as many as 3,073

6. A cafeteria makes 2,516 pounds of white rice and 608 pounds of brown rice every month. After 6 months, how many pounds of rice does the cafeteria make?
Lesson 12: Solve two-step word problems, including multiplicative comparison.

Name ________________________________  Date __________________

Use the RDW process to solve the following problems.

1. The table shows the cost of party favors. Each party guest receives a bag with 1 balloon, 1 lollipop, and 1 bracelet. What is the total cost for 9 guests?

<table>
<thead>
<tr>
<th>Item</th>
<th>Cost</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 balloon</td>
<td>26¢</td>
</tr>
<tr>
<td>1 lollipop</td>
<td>14¢</td>
</tr>
<tr>
<td>1 bracelet</td>
<td>33¢</td>
</tr>
</tbody>
</table>

2. The Turner family uses 548 liters of water per day. The Hill family uses 3 times as much water per day. How much water does the Hill family use per week?

3. Jayden has 347 marbles. Elvis has 4 times as many as Jayden. Presley has 799 fewer than Elvis. How many marbles does Presley have?
4. a. Write an equation that would allow someone to find the value of \( R \).

\[
\begin{array}{c|c|c|c}
1,167 & 1,167 & 1,167 & 239 \\
\end{array}
\]

b. Write your own word problem to correspond to the tape diagram, and then solve.
Lesson 12: Solve two-step word problems, including multiplicative comparison.

Use the RDW process to solve the following problems.

1. The table shows the number of stickers of various types in Chrissy’s new sticker book. Chrissy’s six friends each own the same sticker book. How many stickers do Chrissy and her six friends have altogether?

<table>
<thead>
<tr>
<th>Type of Sticker</th>
<th>Number of Stickers</th>
</tr>
</thead>
<tbody>
<tr>
<td>flowers</td>
<td>32</td>
</tr>
<tr>
<td>smiley faces</td>
<td>21</td>
</tr>
<tr>
<td>hearts</td>
<td>39</td>
</tr>
</tbody>
</table>

2. The small copier makes 437 copies each day. The large copier makes 4 times as many copies each day. How many copies does the large copier make each week?

3. Jared sold 194 Boy Scout chocolate bars. Matthew sold three times as many as Jared. Gary sold 297 fewer than Matthew. How many bars did Gary sell?
4. a. Write an equation that would allow someone to find the value of M.

\[
\begin{align*}
973 \text{ meters} \\
723 \text{ meters} & \quad 723 \text{ meters} \\
\hline
\end{align*}
\]

b. Write your own word problem to correspond to the tape diagram, and then solve.
Lesson 13: Use multiplication, addition, or subtraction to solve multi-step word problems.

Name ___________________________ Date ___________________

Solve using the RDW process.

1. Over the summer, Kate earned $180 each week for 7 weeks. Of that money, she spent $375 on a new computer and $137 on new clothes. How much money did she have left?

2. Sylvia weighed 8 pounds when she was born. By her first birthday, her weight had tripled. By her second birthday, she had gained 12 more pounds. At that time, Sylvia’s father weighed 5 times as much as she did. What was Sylvia and her dad’s combined weight?
3. Three boxes weighing 128 pounds each and one box weighing 254 pounds were loaded onto the back of an empty truck. A crate of apples was then loaded onto the same truck. If the total weight loaded onto the truck was 2,000 pounds, how much did the crate of apples weigh?

4. In one month, Charlie read 814 pages. In the same month, his mom read 4 times as many pages as Charlie, and that was 143 pages more than Charlie’s dad read. What was the total number of pages read by Charlie and his parents?
Solve using the RDW process.

1. A pair of jeans costs $89. A jean jacket costs twice as much. What is the total cost of a jean jacket and 4 pairs of jeans?

2. Sarah bought a shirt on sale for $35. The original price of the shirt was 3 times that amount. Sarah also bought a pair of shoes on sale for $28. The original price of the shoes was 5 times that amount. Together, how much money did the shirt and shoes cost before they went on sale?
3. All 3,000 seats in a theater are being replaced. So far, 5 sections of 136 seats and a sixth section containing 348 seats have been replaced. How many more seats do they still need to replace?

4. Computer Depot sold 762 reams of paper. Paper Palace sold 3 times as much paper as Computer Depot and 143 reams more than Office Supply Central. How many reams of paper were sold by all three stores combined?
Lesson 14: Solve division word problems with remainders.

Name _____________________________ Date ______________________

Use the RDW process to solve the following problems.

1. There are 19 identical socks. How many pairs of socks are there? Will there be any socks without a match? If so, how many?

2. If it takes 8 inches of ribbon to make a bow, how many bows can be made from 3 feet of ribbon (1 foot = 12 inches)? Will any ribbon be left over? If so, how much?

3. The library has 27 chairs and 5 tables. If the same number of chairs is placed at each table, how many chairs can be placed at each table? Will there be any extra chairs? If so, how many?
4. The baker has 42 kilograms of flour. She uses 8 kilograms each day. After how many days will she need to buy more flour?

5. Caleb has 76 apples. He wants to bake as many pies as he can. If it takes 8 apples to make each pie, how many apples will he use? How many apples will not be used?

6. Forty-five people are going to the beach. Seven people can ride in each van. How many vans will be required to get everyone to the beach?
Lesson 14 Homework

Name ___________________________ Date __________________

Use the RDW process to solve the following problems.

1. Linda makes booklets using 2 sheets of paper. She has 17 sheets of paper. How many of these booklets can she make? Will she have any extra paper? How many sheets?

2. Linda uses thread to sew the booklets together. She cuts 6 inches of thread for each booklet. How many booklets can she stitch with 50 inches of thread? Will she have any unused thread after stitching up the booklets? If so, how much?

3. Ms. Rochelle wants to put her 29 students into groups of 6. How many groups of 6 can she make? If she puts any remaining students in a smaller group, how many students will be in that group?
4. A trainer gives his horse, Caballo, 7 gallons of water every day from a 57-gallon container. How many days will Caballo receive his full portion of water from the container? On which number day will the trainer need to refill the container of water?

5. Meliza has 43 toy soldiers. She lines them up in rows of 5 to fight imaginary zombies. How many of these rows can she make? After making as many rows of 5 as she can, she puts the remaining soldiers in the last row. How many soldiers are in that row?

6. Seventy-eight students are separated into groups of 8 for a field trip. How many groups are there? The remaining students form a smaller group of how many students?
Lesson 15: Understand and solve division problems with a remainder using the array and area models.

<table>
<thead>
<tr>
<th>Show division using an array.</th>
<th>Show division using an area model.</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. 18 ÷ 6</td>
<td></td>
</tr>
<tr>
<td>Quotient = _________</td>
<td>Can you show 18 ÷ 6 with one rectangle? ______</td>
</tr>
<tr>
<td>Remainder = _______</td>
<td></td>
</tr>
</tbody>
</table>

| 2. 19 ÷ 6                    |                                   |
| Quotient = _________          | Can you show 19 ÷ 6 with one rectangle? ______ |
| Remainder = _______           | Explain how you showed the remainder: |
Lesson 15: Understand and solve division problems with a remainder using the array and area models.

1. **Example:** \(25 \div 2\)
   - a. \[\begin{array}{cccccccccccccccc}
   \hline
   \hline
   & & & & & & & & & & & & & & & & \\
   \hline
   \hline
   \end{array}\]
   - b. \[\begin{array}{cccccccccccccccc}
   \hline
   \hline
   \hline
   \hline
   \end{array}\]
   - Quotient = 12  Remainder = 1

2. **3.** \(29 \div 3\)
   - a. 
   - b. 

3. **4.** \(22 \div 5\)
   - a. 
   - b. 

4. **5.** \(43 \div 4\)
   - a. 
   - b. 

5. **6.** \(59 \div 7\)
   - a. 
   - b. 

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EUREKA MATH 4•3
Lesson 15: Understand and solve division problems with a remainder using the array and area models.

<table>
<thead>
<tr>
<th>Show division using an array.</th>
<th>Show division using an area model.</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. 24 ÷ 4</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td>Quotient = _______</td>
<td>Can you show 24 ÷ 4 with one rectangle? ______</td>
</tr>
<tr>
<td>Remainder = _______</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td>2. 25 ÷ 4</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td>Quotient = _______</td>
<td>Can you show 25 ÷ 4 with one rectangle? ______</td>
</tr>
<tr>
<td>Remainder = _______</td>
<td>Explain how you showed the remainder:</td>
</tr>
</tbody>
</table>

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G4-M3-SE-1.1.0-06.2015
Solve using an array and area model. The first one is done for you.

Example: 25 ÷ 3

a. 

Quotient = 8  Remainder = 1

3. 44 ÷ 7

a. 

b. 

4. 34 ÷ 6

a. 

b. 

5. 37 ÷ 6

a. 

b. 

6. 46 ÷ 8

a. 

b.
Lesson 16: Understand and solve two-digit dividend division problems with a remainder in the ones place by using place value disks.

Show the division using disks. Relate your work on the place value chart to long division. Check your quotient and remainder by using multiplication and addition.

1. \(7 ÷ 2\)

   \[
   \begin{array}{c|c}
   \text{Tens} & \text{Ones} \\
   \hline
   & 7 \\
   \end{array}
   \]

   \[
   \begin{array}{c}
   2 \longdiv{7} \\
   \hline
   \end{array}
   \]

   Check Your Work

   \[
   \begin{array}{c}
   \times 2 \\
   \hline
   \\
   \end{array}
   \]

   \[
   \begin{array}{c}
   \text{quotient} = \underline{} \\
   \text{remainder} = \underline{}
   \end{array}
   \]

2. \(27 ÷ 2\)

   \[
   \begin{array}{c|c}
   \text{Tens} & \text{Ones} \\
   \hline
   & 27 \\
   \end{array}
   \]

   \[
   \begin{array}{c}
   2 \longdiv{27} \\
   \hline
   \end{array}
   \]

   Check Your Work

   \[
   \begin{array}{c}
   \text{quotient} = \underline{} \\
   \text{remainder} = \underline{}
   \end{array}
   \]
Lesson 16 Problem Set

3. \(8 \div 3\)

<table>
<thead>
<tr>
<th>Ones</th>
</tr>
</thead>
<tbody>
<tr>
<td>_</td>
</tr>
</tbody>
</table>

\[
3 \longdiv{8} 
\]

quotient = __________

remainder = __________

4. \(38 \div 3\)

<table>
<thead>
<tr>
<th>Tens</th>
<th>Ones</th>
</tr>
</thead>
<tbody>
<tr>
<td>_</td>
<td>_</td>
</tr>
</tbody>
</table>

\[
3 \longdiv{38} 
\]

quotient = __________

remainder = __________
5. \( 6 \div 4 \)

<table>
<thead>
<tr>
<th>Ones</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
</tr>
</tbody>
</table>

\[
\begin{array}{c|c}
\text{Tens} & \text{Ones} \\
\hline
4 & 6 \\
\end{array}
\]

quotient = _____________
remainder = _____________

Check Your Work

6. \( 86 \div 4 \)

<table>
<thead>
<tr>
<th>Tens</th>
<th>Ones</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
</tr>
</tbody>
</table>

\[
\begin{array}{c|c}
\text{Tens} & \text{Ones} \\
\hline
4 & 86 \\
\end{array}
\]

quotient = _____________
remainder = _____________

Check Your Work
Lesson 16 Homework

Name ____________________________ Date _______________

Show the division using disks. Relate your work on the place value chart to long division. Check your quotient and remainder by using multiplication and addition.

1. \(7 \div 3\)
   \[
   \begin{array}{c|c}
   \text{Tens} & \text{Ones} \\
   \hline
   & 3 \left[\begin{array}{c}
   \text{餘} \left(7\right)
   \end{array}\right]
   \end{array}
   \]
   \[
   \begin{array}{c}
   \text{Check Your Work}
   \end{array}
   \]
   \[
   \begin{array}{c}
   \text{quotient} = \_
   \end{array}
   \]
   \[
   \begin{array}{c}
   \text{remainder} = \_
   \end{array}
   \]

2. \(67 \div 3\)
   \[
   \begin{array}{c|c}
   \text{Tens} & \text{Ones} \\
   \hline
   & 3 \left[\begin{array}{c}
   \text{餘} \left(67\right)
   \end{array}\right]
   \end{array}
   \]
   \[
   \begin{array}{c}
   \text{Check Your Work}
   \end{array}
   \]
   \[
   \begin{array}{c}
   \text{quotient} = \_
   \end{array}
   \]
   \[
   \begin{array}{c}
   \text{remainder} = \_
   \end{array}
   \]
3. 5 ÷ 2

<table>
<thead>
<tr>
<th>Ones</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
</tr>
</tbody>
</table>

\[ 2 \overline{\div} 5 \]

quotient = __________
remainder = __________

4. 85 ÷ 2

<table>
<thead>
<tr>
<th>Tens</th>
<th>Ones</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
</tr>
</tbody>
</table>

\[ 2 \overline{\div} 85 \]

quotient = __________
remainder = __________
Lesson 16: Understand and solve two-digit dividend division problems with a remainder in the ones place by using place value disks.

5. $5 \div 4$

\[
\begin{array}{c|c}
\text{Tens} & \text{Ones} \\
\hline
 & \\
\end{array}
\]

\[
\begin{array}{c}
4 \overline{\times}
\
\hline
5
\end{array}
\]

quotient = ________

remainder = ________

Check Your Work

6. $85 \div 4$

\[
\begin{array}{c|c}
\text{Tens} & \text{Ones} \\
\hline
 & \\
\end{array}
\]

\[
\begin{array}{c}
4 \overline{\times}
\
\hline
8 \ 5
\end{array}
\]

quotient = ________

remainder = ________

Check Your Work
Lesson 16: Understand and solve two-digit dividend division problems with a remainder in the ones place by using place value disks.

<table>
<thead>
<tr>
<th>ones</th>
<th>tens place value chart</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Name ______________________________ Date __________________

Show the division using disks. Relate your model to long division. Check your quotient and remainder by using multiplication and addition.

1. $5 \div 2$

\[
\begin{array}{c|c}
\text{Tens} & \text{Ones} \\
\hline
 & 5 \\
\end{array}
\]

Check Your Work

\[
\begin{array}{c}
2 \\
\times 2 \\
\end{array}
\]

quotient = __________
remainder = __________

2. $50 \div 2$

\[
\begin{array}{c|c}
\text{Tens} & \text{Ones} \\
\hline
 & 50 \\
\end{array}
\]

Check Your Work

\[
\begin{array}{c}
2 \\
\end{array}
\]

quotient = __________
remainder = __________
3. $7 \div 3$

<table>
<thead>
<tr>
<th>Ones</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
</tr>
</tbody>
</table>

\[3 \longdiv{7}\]

quotient = __________
remainder = __________

4. $75 \div 3$

<table>
<thead>
<tr>
<th>Tens</th>
<th>Ones</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
</tr>
</tbody>
</table>

\[3 \longdiv{75}\]

quotient = __________
remainder = __________
5. \( 9 \div 4 \)

\[
\begin{array}{c|c}
\text{Tens} & \text{Ones} \\
\hline
4 & 9
\end{array}
\]

Check Your Work

quotient = ________

remainder = ________

6. \( 92 \div 4 \)

\[
\begin{array}{c|c}
\text{Tens} & \text{Ones} \\
\hline
4 & 9 \ 2
\end{array}
\]

Check Your Work

quotient = ______

remainder = _____
Show the division using disks. Relate your model to long division. Check your quotient and remainder by using multiplication and addition.

1. \(7 \div 2\)

   \[
   \begin{array}{c|c}
   \text{Ones} & 7 \\
   \hline
   \end{array}
   \]

   \[
   \begin{array}{c|c}
   2 & \leftarrow \text{quotient}
   \\
   \hline
   \\
   \end{array}
   \]

   \begin{align*}
   \text{quotient} &= \_\_\_\_ \\
   \text{remainder} &= \_\_\_\_ \\
   \end{align*}

2. \(73 \div 2\)

   \[
   \begin{array}{c|c}
   \text{Tens} & \text{Ones} \\
   \hline
   \\
   \end{array}
   \]

   \[
   \begin{array}{c|c}
   2 & \leftarrow \text{quotient}
   \\
   \hline
   7 & 3
   \\
   \end{array}
   \]

   \begin{align*}
   \text{quotient} &= \_\_\_\_ \\
   \text{remainder} &= \_\_\_\_ \\
   \end{align*}
3. $6 \div 4$

```
\[\begin{array}{c|c}
\text{Tens} & \text{Ones} \\
\hline
4 & 6
\end{array}\]
```

Check Your Work

quotient = 

remainder = 

4. $62 \div 4$

```
\[\begin{array}{c|c}
\text{Tens} & \text{Ones} \\
\hline
4 & 6 2
\end{array}\]
```

Check Your Work

quotient = 

remainder = 

Lesson 17: Represent and solve division problems requiring decomposing a remainder in the tens.
5. \( 8 ÷ 3 \)

\[
\begin{array}{c|c}
\text{Ones} & 3 \div 8 \\
\hline
\end{array}
\]

Check Your Work

quotient = _________

remainder = _________

6. \( 84 ÷ 3 \)

\[
\begin{array}{c|c}
\text{Tens} & \text{Ones} \\
\hline
3 & 8 4 \\
\end{array}
\]

Check Your Work

quotient = _________

remainder = _________
Solve using the standard algorithm. Check your quotient and remainder by using multiplication and addition.

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>1.</td>
<td>$46 \div 2$</td>
</tr>
<tr>
<td>2.</td>
<td>$96 \div 3$</td>
</tr>
<tr>
<td>3.</td>
<td>$85 \div 5$</td>
</tr>
<tr>
<td>4.</td>
<td>$52 \div 4$</td>
</tr>
<tr>
<td>5.</td>
<td>$53 \div 3$</td>
</tr>
<tr>
<td>6.</td>
<td>$95 \div 4$</td>
</tr>
</tbody>
</table>
Lesson 18: Find whole number quotients and remainders.

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>7.</td>
<td>(89 \div 6)</td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td>8.</td>
<td>(96 \div 6)</td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td>9.</td>
<td>(60 \div 3)</td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td>10.</td>
<td>(60 \div 4)</td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td>11.</td>
<td>(95 \div 8)</td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td>12.</td>
<td>(95 \div 7)</td>
</tr>
</tbody>
</table>

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Lesson 18 Homework 4.3

Name ________________________________ Date __________________

Solve using the standard algorithm. Check your quotient and remainder by using multiplication and addition.

1. \( 84 \div 2 \)  
2. \( 84 \div 4 \)

3. \( 48 \div 3 \)  
4. \( 80 \div 5 \)

5. \( 79 \div 5 \)  
6. \( 91 \div 4 \)

Lesson 18: Find whole number quotients and remainders.
Lesson 18 Homework

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>7.</td>
<td>$91 \div 6$</td>
</tr>
<tr>
<td>8.</td>
<td>$91 \div 7$</td>
</tr>
<tr>
<td>9.</td>
<td>$87 \div 3$</td>
</tr>
<tr>
<td>10.</td>
<td>$87 \div 6$</td>
</tr>
<tr>
<td>11.</td>
<td>$94 \div 8$</td>
</tr>
<tr>
<td>12.</td>
<td>$94 \div 6$</td>
</tr>
</tbody>
</table>

Lesson 18: Find whole number quotients and remainders.
1. When you divide 94 by 3, there is a remainder of 1. Model this problem with place value disks. In the place value disk model, how did you show the remainder?

2. Cayman says that 94 ÷ 3 is 30 with a remainder of 4. He reasons this is correct because (3 × 30) + 4 = 94. What mistake has Cayman made? Explain how he can correct his work.
3. The place value disk model is showing $72 \div 3$. Complete the model. Explain what happens to the 1 ten that is remaining in the tens column.

4. Two friends evenly share 56 dollars.
   a. They have 5 ten-dollar bills and 6 one-dollar bills. Draw a picture to show how the bills will be shared. Will they have to make change at any stage?
   b. Explain how they share the money evenly.
1. When you divide 86 by 4, there is a remainder of 2. Model this problem with place value disks. In the place value disk model, how can you see that there is a remainder?

2. Francine says that $86 \div 4$ is 20 with a remainder of 6. She reasons this is correct because $(4 \times 20) + 6 = 86$. What mistake has Francine made? Explain how she can correct her work.
3. The place value disk model is showing $67 \div 4$. Complete the model. Explain what happens to the 2 tens that are remaining in the tens column.

4. Two friends share 76 blueberries.
   a. To count the blueberries, they put them into small bowls of 10 blueberries. Draw a picture to show how the blueberries can be shared equally. Will they have to split apart any of the bowls of 10 blueberries when they share them?
   b. Explain how the friends can share the blueberries fairly.
1. Alfonso solved a division problem by drawing an area model.
   a. Look at the area model. What division problem did Alfonso solve?
      
      ![Area Model Diagram]

      b. Show a number bond to represent Alfonso’s area model. Start with the total, and then show how the total is split into two parts. Below the two parts, represent the total length using the distributive property, and then solve.
      
      \[
      \begin{align*}
      \text{Total} & = 40 + 32 \\
      \text{Part 1} & = \text{Length} \\
      \text{Part 2} & = \text{Length} \\
      \end{align*}
      \]

      \[
      \begin{align*}
      \text{Total} & = \text{Part 1} + \text{Part 2} \\
      \text{Total} & = \text{Length} + \text{Length} \\
      \end{align*}
      \]

2. Solve 45 \(\div\) 3 using an area model. Draw a number bond, and use the distributive property to solve for the unknown length.
3. Solve $64 \div 4$ using an area model. Draw a number bond to show how you partitioned the area, and represent the division with a written method.

4. Solve $92 \div 4$ using an area model. Explain, using words, pictures, or numbers, the connection of the distributive property to the area model.

5. Solve $72 \div 6$ using an area model and the standard algorithm.
1. Maria solved a division problem by drawing an area model.
   a. Look at the area model. What division problem did Maria solve?

   ![Area Model]

   b. Show a number bond to represent Maria’s area model. Start with the total, and then show how the total is split into two parts. Below the two parts, represent the total length using the distributive property, and then solve.

   ![Number Bond]

   \[ (\_\div\_) + (\_\div\_) = \_ + \_ = \_ \]

2. Solve \(42 \div 3\) using an area model. Draw a number bond, and use the distributive property to solve for the unknown length.
3. Solve $60 \div 4$ using an area model. Draw a number bond to show how you partitioned the area, and represent the division with a written method.

4. Solve $72 \div 4$ using an area model. Explain, using words, pictures, or numbers, the connection of the distributive property to the area model.

5. Solve $96 \div 6$ using an area model and the standard algorithm.
Lesson 21 Problem Set

Name ________________________________ Date __________________

1. Solve $37 \div 2$ using an area model. Use long division and the distributive property to record your work.

2. Solve $76 \div 3$ using an area model. Use long division and the distributive property to record your work.

3. Carolina solved the following division problem by drawing an area model.

![Area model diagram]

a. What division problem did she solve?

b. Show how Carolina’s model can be represented using the distributive property.
Solve the following problems using the area model. Support the area model with long division or the distributive property.

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>4.</td>
<td>$48 \div 3$</td>
</tr>
<tr>
<td>5.</td>
<td>$49 \div 3$</td>
</tr>
<tr>
<td>6.</td>
<td>$56 \div 4$</td>
</tr>
<tr>
<td>7.</td>
<td>$58 \div 4$</td>
</tr>
<tr>
<td>8.</td>
<td>$66 \div 5$</td>
</tr>
<tr>
<td>9.</td>
<td>$79 \div 3$</td>
</tr>
</tbody>
</table>
10. Seventy-three students are divided into groups of 6 students each. How many groups of 6 students are there? How many students will not be in a group of 6?
1. Solve $35 \div 2$ using an area model. Use long division and the distributive property to record your work.

2. Solve $79 \div 3$ using an area model. Use long division and the distributive property to record your work.

3. Paulina solved the following division problem by drawing an area model.

![Area Model Diagram]

a. What division problem did she solve?

b. Show how Paulina’s model can be represented using the distributive property.
Solve the following problems using the area model. Support the area model with long division or the distributive property.

4. \(42 \div 3\)  
5. \(43 \div 3\)  
6. \(52 \div 4\)  
7. \(54 \div 4\)  
8. \(61 \div 5\)  
9. \(73 \div 3\)  

Lesson 21: Solve division problems with remainders using the area model.
10. Ninety-seven lunch trays were placed equally in 4 stacks. How many lunch trays were in each stack? How many lunch trays will be left over?
Name ____________________________________________  Date __________________

1. Record the factors of the given numbers as multiplication sentences and as a list in order from least to greatest. Classify each as prime (P) or composite (C). The first problem is done for you.

<table>
<thead>
<tr>
<th>Multiplication Sentences</th>
<th>Factors</th>
<th>P or C</th>
</tr>
</thead>
<tbody>
<tr>
<td>a. $4$</td>
<td>$1 \times 4 = 4$, $2 \times 2 = 4$</td>
<td>The factors of 4 are: 1, 2, 4</td>
</tr>
<tr>
<td>b. $6$</td>
<td></td>
<td>The factors of 6 are:</td>
</tr>
<tr>
<td>c. $7$</td>
<td></td>
<td>The factors of 7 are:</td>
</tr>
<tr>
<td>d. $9$</td>
<td></td>
<td>The factors of 9 are:</td>
</tr>
<tr>
<td>e. $12$</td>
<td></td>
<td>The factors of 12 are:</td>
</tr>
<tr>
<td>f. $13$</td>
<td></td>
<td>The factors of 13 are:</td>
</tr>
<tr>
<td>g. $15$</td>
<td></td>
<td>The factors of 15 are:</td>
</tr>
<tr>
<td>h. $16$</td>
<td></td>
<td>The factors of 16 are:</td>
</tr>
<tr>
<td>i. $18$</td>
<td></td>
<td>The factors of 18 are:</td>
</tr>
<tr>
<td>j. $19$</td>
<td></td>
<td>The factors of 19 are:</td>
</tr>
<tr>
<td>k. $21$</td>
<td></td>
<td>The factors of 21 are:</td>
</tr>
<tr>
<td>l. $24$</td>
<td></td>
<td>The factors of 24 are:</td>
</tr>
</tbody>
</table>
2. Find all factors for the following numbers, and classify each number as prime or composite. Explain your classification of each as prime or composite.

<table>
<thead>
<tr>
<th>Factor Pairs for 25</th>
<th>Factor Pairs for 28</th>
<th>Factor Pairs for 29</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
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<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

3. Bryan says all prime numbers are odd numbers.
   a. List all of the prime numbers less than 20 in numerical order.
   b. Use your list to show that Bryan’s claim is false.

4. Sheila has 28 stickers to divide evenly among 3 friends. She thinks there will be no leftovers. Use what you know about factor pairs to explain if Sheila is correct.
1. Record the factors of the given numbers as multiplication sentences and as a list in order from least to greatest. Classify each as prime (P) or composite (C). The first problem is done for you.

<table>
<thead>
<tr>
<th>Multiplication Sentences</th>
<th>Factors</th>
<th>P or C</th>
</tr>
</thead>
<tbody>
<tr>
<td>a. 8</td>
<td>The factors of 8 are: 1, 2, 4, 8</td>
<td>C</td>
</tr>
<tr>
<td>1 × 4 = 8</td>
<td>2 × 4 = 8</td>
<td></td>
</tr>
<tr>
<td>b. 10</td>
<td>The factors of 10 are:</td>
<td></td>
</tr>
<tr>
<td>c. 11</td>
<td>The factors of 11 are:</td>
<td></td>
</tr>
<tr>
<td>d. 14</td>
<td>The factors of 14 are:</td>
<td></td>
</tr>
<tr>
<td>e. 17</td>
<td>The factors of 17 are:</td>
<td></td>
</tr>
<tr>
<td>f. 20</td>
<td>The factors of 20 are:</td>
<td></td>
</tr>
<tr>
<td>g. 22</td>
<td>The factors of 22 are:</td>
<td></td>
</tr>
<tr>
<td>h. 23</td>
<td>The factors of 23 are:</td>
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<td>i. 25</td>
<td>The factors of 25 are:</td>
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<td>j. 26</td>
<td>The factors of 26 are:</td>
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<td>k. 27</td>
<td>The factors of 27 are:</td>
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<tr>
<td>l. 28</td>
<td>The factors of 28 are:</td>
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</table>
2. Find all factors for the following numbers, and classify each number as prime or composite. Explain your classification of each as prime or composite.

<table>
<thead>
<tr>
<th>Factor Pairs for 19</th>
<th>Factor Pairs for 21</th>
<th>Factor Pairs for 24</th>
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</table>

3. Bryan says that only even numbers are composite.
   a. List all of the odd numbers less than 20 in numerical order.
   b. Use your list to show that Bryan’s claim is false.

4. Julie has 27 grapes to divide evenly among 3 friends. She thinks there will be no leftovers. Use what you know about factor pairs to explain whether or not Julie is correct.
1. Explain your thinking or use division to answer the following.

<p>| | |</p>
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<thead>
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<tbody>
<tr>
<td>a.</td>
<td>Is 2 a factor of 84?</td>
</tr>
<tr>
<td>c.</td>
<td>Is 3 a factor of 84?</td>
</tr>
<tr>
<td>e.</td>
<td>Is 6 a factor of 84?</td>
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<tr>
<td>g.</td>
<td>Is 5 a factor of 84?</td>
</tr>
</tbody>
</table>
2. Use the associative property to find more factors of 24 and 36.

   a. 24 = 12 \times 2
      = (___ \times 3) \times 2
      = ___ \times (3 \times 2)
      = ___ \times 6
      = ___

   b. 36 = ____ \times 4
      = (___ \times 3) \times 4
      = ___ \times (3 \times 4)
      = ___ \times 12
      = ___

3. In class, we used the associative property to show that when 6 is a factor, then 2 and 3 are factors, because 6 = 2 \times 3. Use the fact that 8 = 4 \times 2 to show that 2 and 4 are factors of 56, 72, and 80.

   56 = 8 \times 7
   72 = 8 \times 9
   80 = 8 \times 10

4. The first statement is false. The second statement is true. Explain why, using words, pictures, or numbers.

   If a number has 2 and 4 as factors, then it has 8 as a factor.
   If a number has 8 as a factor, then both 2 and 4 are factors.
Lesson 23 Homework

1. Explain your thinking or use division to answer the following.

   a. Is 2 a factor of 72?  
   b. Is 2 a factor of 73?  

   c. Is 3 a factor of 72?  
   d. Is 2 a factor of 60?  

   e. Is 6 a factor of 72?  
   f. Is 4 a factor of 60?  

   g. Is 5 a factor of 72?  
   h. Is 8 a factor of 60?
2. Use the associative property to find more factors of 12 and 30.

   a. \[12 = 6 \times 2\]
      \[= (\_\_ \times 2) \times 2\]
      \[= \_\_ \times (2 \times 2)\]
      \[= \_\_ \times \_\_\]
      \[= \_\_\]

   b. \[30 = \_\_ \times 5\]
      \[= (\_\_ \times 3) \times 5\]
      \[= \_\_ \times (3 \times 5)\]
      \[= \_\_ \times 15\]
      \[= \_\_\]

3. In class, we used the associative property to show that when 6 is a factor, then 2 and 3 are factors, because \[6 = 2 \times 3\]. Use the fact that \[10 = 5 \times 2\] to show that 2 and 5 are factors of 70, 80, and 90.

   \[70 = 10 \times 7\]
   \[80 = 10 \times 8\]
   \[90 = 10 \times 9\]

4. The first statement is false. The second statement is true. Explain why, using words, pictures, or numbers.

   If a number has 2 and 6 as factors, then it has 12 as a factor.
   If a number has 12 as a factor, then both 2 and 6 are factors.
Lesson 24: Determine if a whole number is a multiple of another number.

1. For each of the following, time yourself for 1 minute. See how many multiples you can write.
   a. Write the multiples of 5 starting from 100.
   b. Write the multiples of 4 starting from 20.
   c. Write the multiples of 6 starting from 36.

2. List the numbers that have 24 as a multiple.

3. Use mental math, division, or the associative property to solve. (Use scratch paper if you like.)
   a. Is 12 a multiple of 4? _____ Is 4 a factor of 12? _____
   b. Is 42 a multiple of 8? _____ Is 8 a factor of 42? _____
   c. Is 84 a multiple of 6? _____ Is 6 a factor of 84? _____

4. Can a prime number be a multiple of any other number except itself? Explain why or why not.
Lesson 24 Problem Set

5. Follow the directions below.

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a. Circle in red the multiples of 2. When a number is a multiple of 2, what are the possible values for the ones digit?

b. Shade in green the multiples of 3. Choose one. What do you notice about the sum of the digits? Choose another. What do you notice about the sum of the digits?

c. Circle in blue the multiples of 5. When a number is a multiple of 5, what are the possible values for the ones digit?

d. Draw an X over the multiples of 10. What digit do all multiples of 10 have in common?
Lesson 24 Homework

1. For each of the following, time yourself for 1 minute. See how many multiples you can write.
   a. Write the multiples of 5 starting from 75.
   b. Write the multiples of 4 starting from 40.
   c. Write the multiples of 6 starting from 24.

2. List the numbers that have 30 as a multiple.

3. Use mental math, division, or the associative property to solve. (Use scratch paper if you like.)
   a. Is 12 a multiple of 3? _____ Is 3 a factor of 12? _____
   b. Is 48 a multiple of 8? _____ Is 48 a factor of 8? _____
   c. Is 56 a multiple of 6? _____ Is 6 a factor of 56? _____

4. Can a prime number be a multiple of any other number except itself? Explain why or why not.
5. Follow the directions below.

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a. Underline the multiples of 6. When a number is a multiple of 6, what are the possible values for the ones digit?

b. Draw a square around the multiples of 4. Look at the multiples of 4 that have an odd number in the tens place. What values do they have in the ones place?

c. Look at the multiples of 4 that have an even number in the tens place. What values do they have in the ones place? Do you think this pattern would continue with multiples of 4 that are larger than 100?

d. Circle the multiples of 9. Choose one. What do you notice about the sum of the digits? Choose another one. What do you notice about the sum of the digits?
Lesson 25: Explore properties of prime and composite numbers to 100 by using multiples.

Name ___________________________ Date ___________________

1. Follow the directions.
   Shade the number 1 red.
   a. Circle the first unmarked number.
   b. Cross off every multiple of that number except the one you circled. If it’s already crossed off, skip it.
   c. Repeat Steps (a) and (b) until every number is either circled or crossed off.
   d. Shade every crossed out number in orange.

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2. a. List the circled numbers.

b. Why were the circled numbers not crossed off along the way?

c. Except for the number 1, what is similar about all of the numbers that were crossed off?

d. What is similar about all of the numbers that were circled?
1. A student used the sieve of Eratosthenes to find all prime numbers less than 100. Create a step-by-step set of directions to show how it was completed. Use the word bank to help guide your thinking as you write the directions. Some words may be used just once, more than once, or not at all.

Directions for completing the sieve of Eratosthenes activity:

Word Bank

- composite
- cross out
- number
- shade
- circle
- X
- multiple
- prime
2. What do all of the numbers that are crossed out have in common?

3. What do all of the circled numbers have in common?

4. There is one number that is neither crossed out nor circled. Why is it treated differently?
Lesson 26 Problem Set 4.3

Name ___________________________ Date __________________

1. Draw place value disks to represent the following problems. Rewrite each in unit form and solve.
   
   a. $6 \div 2 = \underline{\underline{111}}
      
      6 \text{ ones} \div 2 = \underline{\underline{111}} \text{ ones}$

   b. $60 \div 2 = \underline{\underline{111}}
      
      6 \text{ tens} \div 2 = \underline{\underline{111}}$

   c. $600 \div 2 = \underline{\underline{111}}
      
      \underline{\underline{111}} \div 2 = \underline{\underline{111}}$

   d. $6,000 \div 2 = \underline{\underline{111}}
      
      \underline{\underline{111}} \div 2 = \underline{\underline{111}}$

2. Draw place value disks to represent each problem. Rewrite each in unit form and solve.
   
   a. $12 \div 3 = \underline{\underline{111}}
      
      12 \text{ ones} \div 3 = \underline{\underline{111}} \text{ ones}$

   b. $120 \div 3 = \underline{\underline{111}}
      
      \underline{\underline{111}} \div 3 = \underline{\underline{111}}$

   c. $1,200 \div 3 = \underline{\underline{111}}
      
      \underline{\underline{111}} \div 3 = \underline{\underline{111}}$
3. Solve for the quotient. Rewrite each in unit form.

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<td>800 ÷ 2 = 400</td>
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<td>600 ÷ 2 = _______</td>
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<td>8 hundreds ÷ 2 =</td>
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<td>300 ÷ 6 = _______</td>
<td>f.</td>
<td>240 ÷ 4 = _______</td>
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<td>30 tens ÷ 6 = ___ tens</td>
<td>g.</td>
<td>450 ÷ 5 = _______</td>
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<td>i.</td>
<td>3,600 ÷ 4 = _______</td>
<td>j.</td>
<td>2,400 ÷ 4 = _______</td>
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<td>36 hundreds ÷ 4 = ___ hundreds</td>
<td>k.</td>
<td>2,400 ÷ 3 = _______</td>
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<td>l.</td>
<td>4,000 ÷ 5 = _______</td>
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4. Some sand weighs 2,800 kilograms. It is divided equally among 4 trucks. How many kilograms of sand are in each truck?
5. Ivy has 5 times as many stickers as Adrian has. Ivy has 350 stickers. How many stickers does Adrian have?

6. An ice cream stand sold $1,600 worth of ice cream on Saturday, which was 4 times the amount sold on Friday. How much money did the ice cream stand collect on Friday?
Lesson 26: Divide multiples of 10, 100, and 1,000 by single-digit numbers.

Name ___________________________________________  Date ______________________

1. Draw place value disks to represent the following problems. Rewrite each in unit form and solve.

   a.  $6 \div 3 = \underline{\hspace{2cm}}$
      
      $6$ ones $\div 3 = \underline{\hspace{2cm}}$ ones

   b.  $60 \div 3 = \underline{\hspace{2cm}}$
      
      $6$ tens $\div 3 = \underline{\hspace{2cm}}$

   c.  $600 \div 3 = \underline{\hspace{2cm}}$
      
      $\underline{\hspace{4cm}} \div 3 = \underline{\hspace{4cm}}$

   d.  $6,000 \div 3 = \underline{\hspace{2cm}}$
      
      $\underline{\hspace{4cm}} \div 3 = \underline{\hspace{4cm}}$

2. Draw place value disks to represent each problem. Rewrite each in unit form and solve.

   a.  $12 \div 4 = \underline{\hspace{2cm}}$
      
      $12$ ones $\div 4 = \underline{\hspace{2cm}}$ ones

   b.  $120 \div 4 = \underline{\hspace{2cm}}$
      
      $\underline{\hspace{4cm}} \div 4 = \underline{\hspace{4cm}}$

   c.  $1,200 \div 4 = \underline{\hspace{2cm}}$
      
      $\underline{\hspace{4cm}} \div 4 = \underline{\hspace{4cm}}$
3. Solve for the quotient. Rewrite each in unit form.

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<td>b.</td>
<td>900 ÷ 3 =</td>
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<td>8 hundreds ÷ 4 =</td>
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<td>2 hundreds</td>
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<td>e.</td>
<td>200 ÷ 4 =</td>
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<td>f.</td>
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<td>20 tens ÷ 4 =</td>
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<td>12 hundreds ÷ 3 =</td>
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</table>

4. A fleet of 5 fire engines carries a total of 20,000 liters of water. If each truck holds the same amount of water, how many liters of water does each truck carry?
5. Jamie drank 4 times as much juice as Brodie. Jamie drank 280 milliliters of juice. How much juice did Brodie drink?

6. A diner sold $2,400 worth of French fries in June, which was 4 times as much as was sold in May. How many dollars’ worth of French fries were sold at the diner in May?
Lesson 26: Divide multiples of 10, 100, and 1,000 by single-digit numbers.

<table>
<thead>
<tr>
<th>thousands</th>
<th>hundreds</th>
<th>tens</th>
<th>ones</th>
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</thead>
</table>

thousands place value chart for dividing
1. Divide. Use place value disks to model each problem.

a. \(324 \div 2\)

b. \(344 \div 2\)
c. \[483 \div 3\]

d. \[549 \div 3\]
2. Model using place value disks and record using the algorithm.

<p>| | |</p>
<table>
<thead>
<tr>
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<tbody>
<tr>
<td>a. $655 \div 5$</td>
<td><strong>Disks</strong> <strong>Algorithm</strong></td>
</tr>
<tr>
<td>b. $726 \div 3$</td>
<td><strong>Disks</strong> <strong>Algorithm</strong></td>
</tr>
<tr>
<td>c. $688 \div 4$</td>
<td><strong>Disks</strong> <strong>Algorithm</strong></td>
</tr>
</tbody>
</table>
Lesson 27: Represent and solve division problems with up to a three-digit dividend numerically and with place value disks requiring decomposing a remainder in the hundreds place.

Lesson 27 Homework 4.3

Name ________________________________ Date ____________________

1. Divide. Use place value disks to model each problem.

   a. 346 ÷ 2

   b. 528 ÷ 2
Lesson 27: Represent and solve division problems with up to a three-digit dividend numerically and with place value disks requiring decomposing a remainder in the hundreds place.

c. \[ 516 \div 3 \]

d. \[ 729 \div 3 \]
2. Model using place value disks, and record using the algorithm.

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<thead>
<tr>
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<tbody>
<tr>
<td>a.</td>
<td>648 ÷ 4</td>
<td>Disks Algorithm</td>
</tr>
<tr>
<td>b.</td>
<td>755 ÷ 5</td>
<td>Disks Algorithm</td>
</tr>
<tr>
<td>c.</td>
<td>964 ÷ 4</td>
<td>Disks Algorithm</td>
</tr>
</tbody>
</table>

Lesson 27: Represent and solve division problems with up to a three-digit dividend numerically and with place value disks requiring decomposing a remainder in the hundreds place.
Lesson 28 Problem Set

Name ____________________________ Date ___________________

1. Divide. Check your work by multiplying. Draw disks on a place value chart as needed.

   a.  \[ 574 \div 2 \]

   b.  \[ 861 \div 3 \]

   c.  \[ 354 \div 2 \]
Lesson 28: Represent and solve three-digit dividend division with divisors of 2, 3, 4, and 5 numerically.

d. \(354 ÷ 3\)

e. \(873 ÷ 4\)

f. \(591 ÷ 5\)
Lesson 28 Problem Set

<p>| | |</p>
<table>
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<tr>
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<tbody>
<tr>
<td>g.</td>
<td>$275 \div 3$</td>
</tr>
<tr>
<td>h.</td>
<td>$459 \div 5$</td>
</tr>
<tr>
<td>i.</td>
<td>$678 \div 4$</td>
</tr>
</tbody>
</table>
Lesson 28: Represent and solve three-digit dividend division with divisors of 2, 3, 4, and 5 numerically.

j. $955 \div 4$

2. Zach filled 581 one-liter bottles with apple cider. He distributed the bottles to 4 stores. Each store received the same number of bottles. How many liter bottles did each of the stores receive? Were there any bottles left over? If so, how many?
1. Divide. Check your work by multiplying. Draw disks on a place value chart as needed.

a. \( 378 \div 2 \)

b. \( 795 \div 3 \)

c. \( 512 \div 4 \)
d. \[ 492 \div 4 \]

e. \[ 539 \div 3 \]

f. \[ 862 \div 5 \]
<p>| | |</p>
<table>
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</table>
g. 498 ÷ 3 |   |
h. 783 ÷ 5 |   |
i. 621 ÷ 4 |   |
2. Selena’s dog completed an obstacle course that was 932 meters long. There were 4 parts to the course, all equal in length. How long was 1 part of the course?
1. Divide, and then check using multiplication.

   a. \(1,672 \div 4\)

   b. \(1,578 \div 4\)

   c. \(6,948 \div 2\)
Lesson 29: Represent numerically four-digit dividend division with divisors of 2, 3, 4, and 5, decomposing a remainder up to three times.

d. \(8,949 \div 4\)

e. \(7,569 \div 2\)

f. \(7,569 \div 3\)
<p>| | |</p>
<table>
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</table>
g.  | $7,955 ÷ 5$  |
h.  | $7,574 ÷ 5$  |
i.  | $7,469 ÷ 3$  |
j.  $9,956 \div 4$

2. There are twice as many cows as goats on a farm. All the cows and goats have a total of 1,116 legs. How many goats are there?
Lesson 29: Represent numerically four-digit dividend division with divisors of 2, 3, 4, and 5, decomposing a remainder up to three times.

Lesson 29 Homework

Name ____________________________ Date __________________

1. Divide, and then check using multiplication.

a. \( 2,464 \div 4 \)

b. \( 1,848 \div 3 \)

c. \( 9,426 \div 3 \)
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<table>
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<tr>
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<tbody>
<tr>
<td>d.</td>
<td>6,587 ÷ 2</td>
<td></td>
</tr>
<tr>
<td>e.</td>
<td>5,445 ÷ 3</td>
<td></td>
</tr>
<tr>
<td>f.</td>
<td>5,425 ÷ 2</td>
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</tbody>
</table>
g. $8,467 \div 3$ &   

<p>| | |</p>
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</table>
h. $8,456 \div 3$ &   

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</table>
i. $4,937 \div 4$ &   

Lesson 29: Represent numerically four-digit dividend division with divisors of 2, 3, 4, and 5, decomposing a remainder up to three times.
j. \( 6,173 \div 5 \)

2. A truck has 4 crates of apples. Each crate has an equal number of apples. Altogether, the truck is carrying 1,728 apples. How many apples are in 3 crates?
Lesson 30: Solve division problems with a zero in the dividend or with a zero in the quotient.

Divide. Check your solutions by multiplying.

1. \(204 \div 4\)  
2. \(704 \div 3\)  
3. \(627 \div 3\)  
4. \(407 \div 2\)
Lesson 30: Solve division problems with a zero in the dividend or with a zero in the quotient.

5. \( 760 \div 4 \)  
6. \( 5,120 \div 4 \)

7. \( 3,070 \div 5 \)  
8. \( 6,706 \div 5 \)
Lesson 30 Problem Set

9. \(8,313 \div 4\)  
10. \(9,008 \div 3\)

11. a. Find the quotient and remainder for \(3,131 \div 3\).

b. How could you change the digit in the ones place of the whole so that there would be no remainder? Explain how you determined your answer.
Lesson 30: Solve division problems with a zero in the dividend or with a zero in the quotient.

Divide. Check your solutions by multiplying.

1. $409 \div 5$
2. $503 \div 2$
3. $831 \div 4$
4. $602 \div 3$
Lesson 30: Solve division problems with a zero in the dividend or with a zero in the quotient.

5. \(720 \div 3\)  
6. \(6,250 \div 5\)

7. \(2,060 \div 5\)  
8. \(9,031 \div 2\)
9. \(6,218 \div 4\)  
10. \(8,000 \div 4\)
Name ____________________________  Date __________________

Draw a tape diagram and solve. The first two tape diagrams have been drawn for you. Identify if the group size or the number of groups is unknown.

1. Monique needs exactly 4 plates on each table for the banquet. If she has 312 plates, how many tables is she able to prepare?

   \[
   \begin{array}{c}
   \text{312} \\
   \hline
   \text{4} \\
   \hline
   \text{?} \\
   \end{array}
   \]

2. 2,365 books were donated to an elementary school. If 5 classrooms shared the books equally, how many books did each class receive?

   \[
   \begin{array}{c}
   \text{2,365} \\
   \hline
   \text{?} \\
   \end{array}
   \]

3. If 1,503 kilograms of rice was packed in sacks weighing 3 kilograms each, how many sacks were packed?
Lesson 31: Interpret division word problems as either \textit{number of groups unknown} or \textit{group size unknown}

4. Rita made 5 batches of cookies. There was a total of 2,400 cookies. If each batch contained the same number of cookies, how many cookies were in 4 batches?

5. Every day, Sarah drives the same distance to work and back home. If Sarah drove 1,005 miles in 5 days, how far did Sarah drive in 3 days?
Lesson 31 Homework

Name __________________________________________ Date ____________________

Solve the following problems. Draw tape diagrams to help you solve. Identify if the group size or the number of groups is unknown.

1. 500 milliliters of juice was shared equally by 4 children. How many milliliters of juice did each child get?

2. Kelly separated 618 cookies into baggies. Each baggie contained 3 cookies. How many baggies of cookies did Kelly make?

3. Jeff biked the same distance each day for 5 days. If he traveled 350 miles altogether, how many miles did he travel each day?
4. A piece of ribbon 876 inches long was cut by a machine into 4-inch long strips to be made into bows. How many strips were cut?

5. Five Martians equally share 1,940 Groblarx fruits. How many Groblarx fruits will 3 of the Martians receive?
Lesson 32: Interpret and find whole number quotients and remainders to solve one-step division word problems with larger divisors of 6, 7, 8, and 9.

Solve the following problems. Draw tape diagrams to help you solve. If there is a remainder, shade in a small portion of the tape diagram to represent that portion of the whole.

1. A concert hall contains 8 sections of seats with the same number of seats in each section. If there are 248 seats, how many seats are in each section?

2. In one day, the bakery made 719 bagels. The bagels were divided into 9 equal shipments. A few bagels were left over and given to the baker. How many bagels did the baker get?

3. The sweet shop has 614 pieces of candy. They packed the candy into bags with 7 pieces in each bag. How many bags of candy did they fill? How many pieces of candy were left?
Lesson 32: Interpret and find whole number quotients and remainders to solve one-step division word problems with larger divisors of 6, 7, 8, and 9.

4. There were 904 children signed up for the relay race. If there were 6 children on each team, how many teams were made? The remaining children served as referees. How many children served as referees?

5. 1,188 kilograms of rice are divided into 7 sacks. How many kilograms of rice are in 6 sacks of rice? How many kilograms of rice remain?
Lesson 32: Interpreting and finding whole number quotients and remainders to solve one-step division word problems with larger divisors of 6, 7, 8, and 9.

Name ____________________________ Date ________________

Solve the following problems. Draw tape diagrams to help you solve. If there is a remainder, shade in a small portion of the tape diagram to represent that portion of the whole.

1. Meneca bought a package of 435 party favors to give to the guests at her birthday party. She calculated that she could give 9 party favors to each guest. How many guests is she expecting?

2. 4,000 pencils were donated to an elementary school. If 8 classrooms shared the pencils equally, how many pencils did each class receive?

3. 2,008 kilograms of potatoes were packed into sacks weighing 8 kilograms each. How many sacks were packed?
4. A baker made 7 batches of muffins. There was a total of 252 muffins. If there was the same number of muffins in each batch, how many muffins were in a batch?

5. Samantha ran 3,003 meters in 7 days. If she ran the same distance each day, how far did Samantha run in 3 days?
1. Ursula solved the following division problem by drawing an area model.

   [Diagram of an area model with the following breakdown:
   400 divided by 4 equals 100, 40 divided by 4 equals 10, and 3 divided by 4 equals 0 remainder 3.]

   a. What division problem did she solve?

   b. Show a number bond to represent Ursula’s area model, and represent the total length using the distributive property.

2. a. Solve 960 ÷ 4 using the area model. There is no remainder in this problem.

   b. Draw a number bond and use the long division algorithm to record your work from Part (a).
3. a. Draw an area model to solve $774 \div 3$.

   b. Draw a number bond to represent this problem.
   c. Record your work using the long division algorithm.

4. a. Draw an area model to solve $1,584 \div 2$.

   b. Draw a number bond to represent this problem.
   c. Record your work using the long division algorithm.
Lesson 33 Homework 4•3

Name ____________________________ Date ______________________

1. Arabelle solved the following division problem by drawing an area model.

   \[ \begin{array}{c}
   \text{4} \\
   \hline
   \text{400} & \text{50} & \text{28} \\
   \text{1600} & \text{200} & \text{20} \\
   \hline
   \text{4} & \text{2} & \text{2} \\
   \end{array} \]

   a. What division problem did she solve?

   b. Show a number bond to represent Arabelle’s area model, and represent the total length using the distributive property.

2. a. Solve 816 ÷ 4 using the area model. There is no remainder in this problem.

   \[ \begin{array}{c}
   \text{816} \\
   \hline
   \text{4} & \text{204} & \text{21} \\
   \text{400} & \text{200} & \text{20} \\
   \hline
   \text{4} & \text{2} & \text{2} \\
   \end{array} \]

   b. Draw a number bond and use a written method to record your work from Part (a).
3. a. Draw an area model to solve $549 \div 3$.

b. Draw a number bond to represent this problem.

c. Record your work using the long division algorithm.

4. a. Draw an area model to solve $2,762 \div 2$.

b. Draw a number bond to represent this problem.

c. Record your work using the long division algorithm.
1. Use the associative property to rewrite each expression. Solve using disks, and then complete the number sentences.

a. $30 \times 24$

\[
= (\underline{\quad} \times 10) \times 24
\]

\[
= \underline{\quad} \times (10 \times 24)
\]

\[
= \underline{\quad}
\]

b. $40 \times 43$

\[
= (4 \times 10) \times \underline{\quad}
\]

\[
= 4 \times (10 \times \underline{\quad})
\]

\[
= \underline{\quad}
\]

c. $30 \times 37$

\[
= (3 \times \underline{\quad}) \times \underline{\quad}
\]

\[
= 3 \times (10 \times \underline{\quad})
\]

\[
= \underline{\quad}
\]
2. Use the associative property and place value disks to solve.
   a. $20 \times 27$
   b. $40 \times 31$

3. Use the associative property without place value disks to solve.
   a. $40 \times 34$
   b. $50 \times 43$

4. Use the distributive property to solve the following problems. Distribute the second factor.
   a. $40 \times 34$
   b. $60 \times 25$
Lesson 34: Multiply two-digit multiples of 10 by two-digit numbers using a place value chart.

1. Use the associative property to rewrite each expression. Solve using disks, and then complete the number sentences.

   a. \(20 \times 34\)
      
      \[
      = (\text{___} \times 10) \times 34
      = \text{___} \times (10 \times 34)
      = \text{_____}
      \]

   b. \(30 \times 34\)
      
      \[
      = (3 \times 10) \times \text{___}
      = 3 \times (10 \times \text{___})
      = \text{_____}
      \]

   c. \(30 \times 42\)
      
      \[
      = (3 \times \text{___}) \times \text{___}
      = 3 \times (10 \times \text{___})
      = \text{_____}
      \]
2. Use the associative property and place value disks to solve.
   a. $20 \times 16$  
   b. $40 \times 32$

3. Use the associative property without place value disks to solve.
   a. $30 \times 21$  
   b. $60 \times 42$

4. Use the distributive property to solve the following. Distribute the second factor.
   a. $40 \times 43$  
   b. $70 \times 23$
Use an area model to represent the following expressions. Then, record the partial products and solve.

1. $20 \times 22$

\[
\begin{array}{c|c}
\hline
\quad & 22 \\
\hline
\times 20 & \\
\hline
\quad & \\
\hline
+ & \\
\hline
\end{array}
\]

2. $50 \times 41$

\[
\begin{array}{c|c}
\hline
\quad & 41 \\
\hline
\times 50 & \\
\hline
\quad & \\
\hline
+ & \\
\hline
\end{array}
\]

3. $60 \times 73$

\[
\begin{array}{c|c}
\hline
\quad & 73 \\
\hline
\times 60 & \\
\hline
\quad & \\
\hline
+ & \\
\hline
\end{array}
\]

Lesson 35: Multiply two-digit multiples of 10 by two-digit numbers using the area model.
Draw an area model to represent the following expressions. Then, record the partial products vertically and solve.

4. $80 \times 32$

5. $70 \times 54$

Visualize the area model, and solve the following expressions numerically.

6. $30 \times 68$

7. $60 \times 34$

8. $40 \times 55$

9. $80 \times 55$
Use an area model to represent the following expressions. Then, record the partial products and solve.

1. \(30 \times 17\)

   \[
   \begin{array}{|c|c|}
   \hline
   17 & \times 30 \\
   \hline
   & + \\
   \hline
   \end{array}
   \]

2. \(40 \times 58\)

   \[
   \begin{array}{|c|c|}
   \hline
   58 & \times 40 \\
   \hline
   & + \\
   \hline
   \end{array}
   \]

3. \(50 \times 38\)

   \[
   \begin{array}{|c|c|}
   \hline
   38 & \times 50 \\
   \hline
   & + \\
   \hline
   \end{array}
   \]
Draw an area model to represent the following expressions. Then, record the partial products vertically and solve.

4. \(60 \times 19\)

5. \(20 \times 44\)

Visualize the area model, and solve the following expressions numerically.

6. \(20 \times 88\)

7. \(30 \times 88\)

8. \(70 \times 47\)

9. \(80 \times 65\)
Lesson 36 Problem Set 4-3

Name ___________________________________________ Date __________________

1. a. In each of the two models pictured below, write the expressions that determine the area of each of the four smaller rectangles.

![Model 1](image1)

![Model 2](image2)

b. Using the distributive property, rewrite the area of the large rectangle as the sum of the areas of the four smaller rectangles. Express first in number form, and then read in unit form.

\[ 14 \times 12 = (4 \times \underline{\hspace{1cm}}) + (4 \times \underline{\hspace{1cm}}) + (10 \times \underline{\hspace{1cm}}) + (10 \times \underline{\hspace{1cm}}) \]

2. Use an area model to represent the following expression. Record the partial products and solve.

\[ 14 \times 22 \]

![Area Model](image3)
Draw an area model to represent the following expressions. Record the partial products vertically and solve.

3. $25 \times 32$

4. $35 \times 42$

Visualize the area model and solve the following numerically using four partial products. (You may sketch an area model if it helps.)

5. $42 \times 11$

6. $46 \times 11$
Name ________________________________ Date __________________

1. a. In each of the two models pictured below, write the expressions that determine the area of each of the four smaller rectangles.

   ![Area Model 1]
   ![Area Model 2]

b. Using the distributive property, rewrite the area of the large rectangle as the sum of the areas of the four smaller rectangles. Express first in number form, and then read in unit form.

   \[13 \times 12 = (3 \times \underline{\hspace{1cm}}) + (3 \times \underline{\hspace{1cm}}) + (10 \times \underline{\hspace{1cm}}) + (10 \times \underline{\hspace{1cm}})\]

Use an area model to represent the following expression. Record the partial products and solve.

2. \[17 \times 34\]
Lesson 36: Multiply two-digit by two-digit numbers using four partial products.

Draw an area model to represent the following expressions. Record the partial products vertically and solve.

3. \(45 \times 18\)  
4. \(45 \times 19\)

Visualize the area model and solve the following numerically using four partial products. (You may sketch an area model if it helps.)

5. \(12 \times 47\)  
6. \(23 \times 93\)

7. \(23 \times 11\)  
8. \(23 \times 22\)
Lesson 37: Transition from four partial products to the standard algorithm for two-digit by two-digit multiplication.

1. Solve \(14 \times 12\) using 4 partial products and 2 partial products. Remember to think in terms of units as you solve. Write an expression to find the area of each smaller rectangle in the area model.

\[
\begin{array}{c}
4 \\
10 \\
\hline
12
\end{array}
\times \begin{array}{c}
1 \\
4
\end{array}
\]

\[
\begin{array}{c}
4 \text{ ones} \times 2 \text{ ones} \\
4 \text{ ones} \times 1 \text{ ten} \\
1 \text{ ten} \times 2 \text{ ones} \\
1 \text{ ten} \times 1 \text{ ten}
\end{array}
\]

2. Solve \(32 \times 43\) using 4 partial products and 2 partial products. Match each partial product to its area on the models. Remember to think in terms of units as you solve.

\[
\begin{array}{c}
4 \\
30 \\
\hline
43
\end{array}
\times \begin{array}{c}
3 \\
2
\end{array}
\]

\[
\begin{array}{c}
2 \text{ ones} \times 3 \text{ ones} \\
2 \text{ ones} \times 4 \text{ tens} \\
3 \text{ tens} \times 3 \text{ ones} \\
3 \text{ tens} \times 4 \text{ tens}
\end{array}
\]

### Notes
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- G4-M3-SE-1.3.D-06.2015
3. Solve $57 \times 15$ using 2 partial products. Match each partial product to its rectangle on the area model.

4. Solve the following using 2 partial products. Visualize the area model to help you.

   a. $25 \times 46$

   b. $18 \times 62$

   c. $39 \times 46$

   d. $78 \times 23$
Lesson 37 Homework

1. Solve $26 \times 34$ using 4 partial products and 2 partial products. Remember to think in terms of units as you solve. Write an expression to find the area of each smaller rectangle in the area model.

   $$
   \begin{array}{c}
   6 \\
   20 \\
   \hline
   30 \quad 4 \\
   \hline
   \end{array}
   \quad \times \quad 
   \begin{array}{c}
   2 \\
   6 \\
   \hline
   \end{array}
   $$

   - $6 \text{ ones} \times 4 \text{ ones}$
   - $6 \text{ ones} \times 3 \text{ tens}$
   - $2 \text{ tens} \times 4 \text{ ones}$
   - $2 \text{ tens} \times 3 \text{ tens}$

2. Solve using 4 partial products and 2 partial products. Remember to think in terms of units as you solve. Write an expression to find the area of each smaller rectangle in the area model.

   $$
   \begin{array}{c}
   2 \\
   80 \\
   \hline
   40 \quad 1 \\
   \hline
   \end{array}
   \quad \times \quad 
   \begin{array}{c}
   8 \\
   2 \\
   \hline
   \end{array}
   $$

   - $2 \text{ ones} \times 1 \text{ one}$
   - $2 \text{ ones} \times 4 \text{ tens}$
   - $8 \text{ tens} \times 1 \text{ one}$
   - $8 \text{ tens} \times 4 \text{ tens}$
3. Solve $52 \times 26$ using 2 partial products and an area model. Match each partial product to its area on the model.

4. Solve the following using 2 partial products. Visualize the area model to help you.

a. 

$$
68 \\
\times 23
$$

b. 

$$
49 \\
\times 33
$$

c. 

$$
16 \\
\times 25
$$

d. 

$$
54 \\
\times 71
$$
1. Express $23 \times 54$ as two partial products using the distributive property. Solve.

$$23 \times 54 = (\_\_ \text{ fifty-fours}) + (\_\_ \text{ fifty-fours})$$

```
  5 4
  x 2 3
```

```
  3 \times \_
   \_
   \_
```

```
20 \times \_
```

2. Express $46 \times 54$ as two partial products using the distributive property. Solve.

$$46 \times 54 = (\_\_ \text{ fifty-fours}) + (\_\_ \text{ fifty-fours})$$

```
  5 4
  x 4 6
```

```
  \_ \times \_
   \_
   \_
```

```
  \_ \times \_
   \_
   \_
```

3. Express $55 \times 47$ as two partial products using the distributive property. Solve.

$$55 \times 47 = (\_\_ \times \_\_) + (\_\_ \times \_\_)$$

```
  4 7
  x 5 5
```

```
  \_ \times \_
   \_
   \_
```

```
  \_ \times \_
   \_
   \_
```
4. Solve the following using 2 partial products.

\[
\begin{array}{c}
58 \\
\times 45 \\
\hline \\
\end{array}
\]

\[
\begin{array}{c}
\quad \times \quad \\
\quad \times \quad \\
\end{array}
\]

5. Solve using the multiplication algorithm.

\[
\begin{array}{c}
82 \\
\times 55 \\
\hline \\
\end{array}
\]

\[
\begin{array}{c}
\quad \times \quad \\
\quad \times \quad \\
\end{array}
\]

6. \( 53 \times 63 \)

7. \( 84 \times 73 \)
Lesson 38:
Transition from four partial products to the standard algorithm for two-digit by two-digit multiplication.

Name ___________________________ Date ______________

1. Express 26 \times 43 as two partial products using the distributive property. Solve.

\[ 26 \times 43 = (___ \text{ forty-threes}) + (___ \text{ forty-threes}) \]

\[ \begin{array}{c}
6 \\
20 \\
\hline
43 \\
\hline
\end{array} \quad \begin{array}{c}
\times 26 \\
\hline
\end{array} \]

\[ 6 \times ___ \\
20 \times ___ \]

2. Express 47 \times 63 as two partial products using the distributive property. Solve.

\[ 47 \times 63 = (___ \text{ sixty-threes}) + (___ \text{ sixty-threes}) \]

\[ \begin{array}{c}
7 \\
40 \\
\hline
63 \\
\hline
\end{array} \quad \begin{array}{c}
\times 47 \\
\hline
\end{array} \]

\[ ___ \times ___ \\
___ \times ___ \]

3. Express 54 \times 67 as two partial products using the distributive property. Solve.

\[ 54 \times 67 = (___ \times ___) + (___ \times ___) \]

\[ \begin{array}{c}
\ \\
\ \\
\hline
67 \\
\hline
\end{array} \quad \begin{array}{c}
\times 54 \\
\hline
\end{array} \]

\[ ___ \times ___ \\
___ \times ___ \]
4. Solve the following using two partial products.

\[
\begin{array}{c}
52 \\
\times \quad 34 \\
\hline \\
\_ \times \_
\end{array}
\]

5. Solve using the multiplication algorithm.

\[
\begin{array}{c}
86 \\
\times \quad 56 \\
\hline \\
\_ \times \_
\end{array}
\]

6. \(54 \times 52\)  

7. \(44 \times 76\)
Lesson 38:
Transition from four partial products to the standard algorithm for two-digit by two digit multiplication.

Lesson 38 Homework

8. $63 \times 63$

9. $68 \times 79$